Modelling Biological Systems with Boolean Networks



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Modelling of biological systems — Example: enzymatic reaction



Modelling of biological systems — Example: enzymatic reaction



$$S + E \iff ES \longrightarrow E + 2 \cdot P$$

constraints: known structure (= domain) and dynamics (= to reproduce)



Many formalisms exist \rightsquigarrow Ulysse Herbarch's presentation

Statistical based on correlations, undirectional



Mechanistic based on the processes, directional Boolean network Bayesian network Process algebras ((b(x,de)[E]) || (B(v, dI)[I])) bh(x, dE) bh(y, dI) (E || I) Differential equation Constraint based model Hybrid systems Petri Nets Interacting state machine Compartment based Agent-based model Cellular automata Rule based ∞

a set of n components (= automata) Boolean status $\mathbb{B} = \{0; 1\}$ n local update functions $f_X : \mathbb{B}^n \to \mathbb{B}$ \neg : "not"; \lor : "or"; \land : "and"



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Boolean network

$$\mathscr{B} = \begin{cases} f_{\mathsf{E}} := \neg \mathsf{E} \\ f_{\mathsf{ES}} := \mathsf{E} \land \mathsf{S} \\ f_{\mathsf{P}} := \mathsf{ES} \land (\neg \mathsf{E} \lor \mathsf{P}) \\ f_{\mathsf{S}} := \neg \mathsf{E} \end{cases}$$

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Boolean network, its interaction graph = structure

$$\mathscr{B} = \begin{cases} f_{\mathsf{E}} := \neg \mathsf{E} & (\mathsf{S}) \xrightarrow{+} (\mathsf{E}) \\ f_{\mathsf{E}\mathsf{S}} := \mathsf{E} \land \mathsf{S} & (\neg \mathsf{E} \lor \mathsf{P}) \\ f_{\mathsf{P}} := \mathsf{E}\mathsf{S} \land (\neg \mathsf{E} \lor \mathsf{P}) & \neg (\mathsf{E}) \xrightarrow{-} (\mathsf{P}) \xrightarrow{+} \\ f_{\mathsf{S}} := \neg \mathsf{E} \end{cases}$$

a set of n components (= automata) Boolean status $\mathbb{B} = \{0; 1\}$ n local update functions $f_X : \mathbb{B}^n \to \mathbb{B}$ \neg : "not"; \lor : "or"; \land : "and"



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Boolean network, its interaction graph and gen. asyn. state transition graph = structure = dynamics



Boolean Networks Synthesis

constraints: known structure (= domain) and dynamics (= to reproduce)





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constraints: known structure (= domain) and dynamics (= to reproduce)



output: (exhaustive set of) BNs compatible with the constraints



1111

And then what?

Analysis on Boolean networks (even large ones !)

- reachability, attractors
- control
- ▶ ...

Despite their simplicity, BNs can fit complex biological phenomena: cell cycle, cancer (breast, bladder, \dots), \dots

Trajectory and attractors — example of biology mapping

Attractors often map to relevant biological properties (physiological state, cellular types, ...).



Dynamical trajectories of the 1.764 protein states (green nodes) flowing to the G1 fixed point (blue node). Arrows between states indicate the direction of dynamic flow from one state to another. The cell-cycle sequence is coloured in blue. The size of a node and the thickness of an arrow are proportional to the logarithm of the traffic flow passing through them.

ightarrow the model fits biology

From "The yeast cell-cycle network is robustly designed." Li et al. 2004

Possible configurations of a system



behaviour of a sane system goes through normal configurations...





collaborators from CRAN: Hélène Dubois-Pot-Schneider, Hélène Dumond, Alex Hirtz and Nolwenn Lebourdais

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Glioblastoma (GBM) affects men twice as much as woman

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Glioblastoma (GBM) affects men twice as much as woman

G-Protein-Coupled Estrogen Receptor (GPER) correlated to survival of GBM patients





low GPFR \rightarrow less survival \rightarrow better survival

high GPER



G-1 (= GPER agonist) blocks GBM cell proliferation in M phase



G-1 (= GPER agonist) blocks GBM cell proliferation in M phase

Can we model this with Boolean networks?

Ongoing project — Boolean network

Extension of an existing BN modelling mammals cell cycle¹ original model: our current model:





¹[Fauré et al. 2006]

Ongoing project — BN dynamics and predictions

Does our BN reproduce biologists observations? Analysis of the synchronous $STG = 2^{11} = 2048$ nodes and edges

- ► dynamics without G-1, with CycD: no perturbation of the cell cycle compared to the original model ✓
- dynamics with G-1, with CycD: cell cycle blocked ✓
- other checks need to be done...

Once all the checks will be passed: Can our BN make useful predictions?

Conclusion

Boolean networks:

- simple, yet powerful formalism to study biological processes
- simple to set up: their construction requires very few data compared to other formalisms
- once built, one can run prediction analysis, control, etc...

Structural & dynamical constraints





Thanks for your attention. Any questions? athenais.vaginay@loria.fr

Enjoy the FCH day!

Our collaborators: Hélène Dubois-Pot-Schneider, Hélène Dumond, Alex Hirtz and Nolwenn Lebourdais

I used some Servier Medical Art in this presentation

$PhD \ Project \qquad \qquad \texttt{1er octobre 2018} \rightarrow \texttt{juin 2022}$

"Selection and analysis of models for biology using knowledge on the domain; application to pathological systems."

